

08/26/15

1.1 Lines in the Plane

Problem

Work

Solution

Find slope

1.  $2x - 5y = 0$

$$\begin{array}{r} 2x - 5y = 0 \\ -2x \quad -2x \\ \hline -5y = -2x \\ -5 \quad -5 \\ \hline y = \frac{2}{5}x \end{array}$$

$m = \frac{2}{5}$

2.  $5x - y = -7$

$$\begin{array}{r} 5x - y = -7 \\ -5x \quad -5x \\ \hline -y = -5x - 7 \\ -1 \quad -1 \quad -1 \\ \hline y = 5x + 7 \end{array}$$

$m = 5$

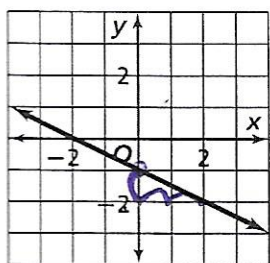
3.

$x - \frac{2}{3}y = \frac{1}{4}$

$$\begin{array}{r} x - \frac{2}{3}y = \frac{1}{4} \\ -x \quad -x \\ \hline \left(\frac{3}{-2}\right) \left(-\frac{2}{3}y\right) = \left(-x + \frac{1}{4}\right) \left(\frac{3}{-2}\right) \\ \hline y = \frac{3}{2}x - \frac{3}{8} \end{array}$$

$m = \frac{3}{2}$

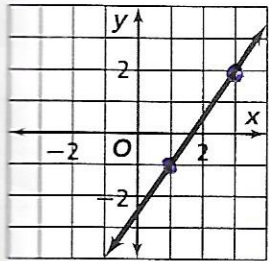
4.



$m = \frac{\text{rise}}{\text{run}} = \frac{-1}{2}$

$m = -\frac{1}{2}$

Since line is decreasing,  
 the slope must be negative



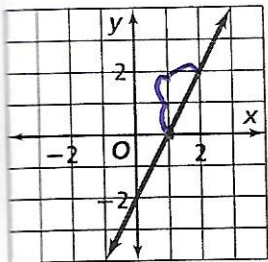
$$x_1, y_1 \quad x_2, y_2$$

$$(1, -1) \text{ and } (3, 2)$$

Since I can find those two points on the graph I can use the formula:

$$m = \frac{3}{2}$$

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{2 - (-1)}{3 - 1} = \frac{3}{2}$$



$$\frac{\text{rise}}{\text{run}} = \frac{2}{1} \quad m = 2$$

$$m = 2$$

7. through

$$x_1, y_1 \quad x_2, y_2$$

$$(4, -1) \text{ and } (-2, -3)$$

$$m = \frac{-3 - (-1)}{-2 - 4} = \frac{-3 + 1}{-2 - 4} = \frac{-2}{-6}$$

$$m = \frac{1}{3}$$

3.  $(3, -5)$  &  
 $(1, 2)$

$$m = \frac{2 - (-5)}{1 - 3} = \frac{7}{-2}$$

$$m = \frac{7}{-2}$$

1. point-slope form.

$$(0, 1) \text{ and } (3, 0)$$

$$m = \frac{0 - 1}{3 - 0} = \frac{-1}{3} \quad x_1, y_1$$

$$(0, 1)$$

$$y - y_1 = m(x - x_1)$$

$$y - 1 = -\frac{1}{3}(x - 0) \quad \text{or} \quad y - 0 = -\frac{1}{3}(x - 3)$$



10.  $(\frac{1}{2}, \frac{2}{3})$

or  $(-\frac{3}{2}, \frac{5}{3})$

$$m = \frac{\frac{5}{3} - \frac{2}{3}}{-\frac{3}{2} - \frac{1}{2}} = \frac{\frac{3}{3}}{-\frac{4}{2}} = \frac{1}{-2}$$

$$m = -\frac{1}{2} \quad y - y_1 = m(x - x_1)$$

$$y - \frac{5}{3} = -\frac{1}{2}(x + \frac{3}{2}) \text{ or } y - \frac{2}{3} = -\frac{1}{2}(x - \frac{1}{2})$$

11.  $(-3, -2)$

or  $(1, 6)$

$$m = \frac{6 - (-2)}{1 - (-3)} = \frac{6 + 2}{1 + 3} = \frac{8}{4} = 2$$

$$y - y_1 = m(x - x_1)$$

$$y + 2 = 2(x + 3) \text{ or } y - 6 = 2(x - 1)$$

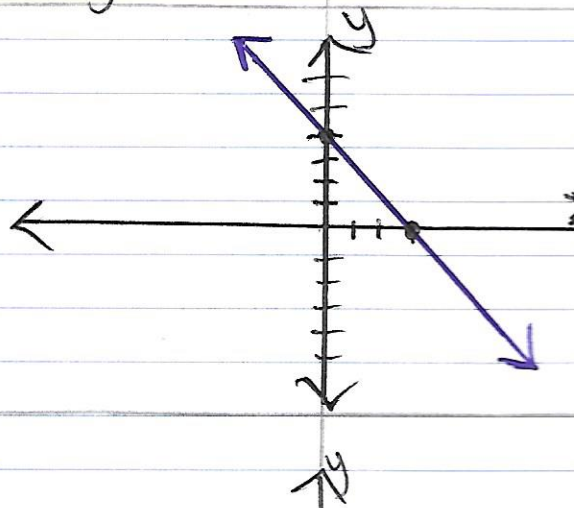
12. Graph

each equation

$$4x + 3y = 12$$

$$\begin{array}{r} 4x + 3y = 12 \\ -4x \phantom{+ 3y} = -4x \\ \hline 3y = -4x + 12 \\ y = -\frac{4}{3}x + 4 \end{array}$$

$$y = -\frac{4}{3}x + 4$$



13.  $\frac{x}{3} - \frac{y}{6} = 1$

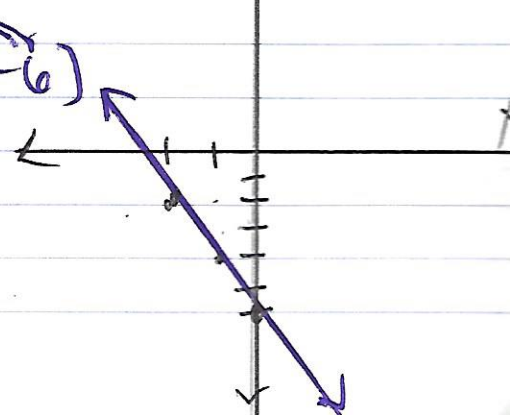
$$\begin{array}{r} \frac{x}{3} - \frac{y}{6} = 1 \\ -\frac{x}{3} \phantom{- \frac{y}{6}} = -\frac{x}{3} \\ \hline (-\frac{y}{6}) = (-\frac{x}{3} + 1) \end{array}$$

$$(-\frac{y}{6}) = (-\frac{x}{3} + 1)(-6)$$

$$y = -\frac{6x}{3} - 6$$

$$y = -2x - 6$$

$$m = -2 \quad b = -6$$

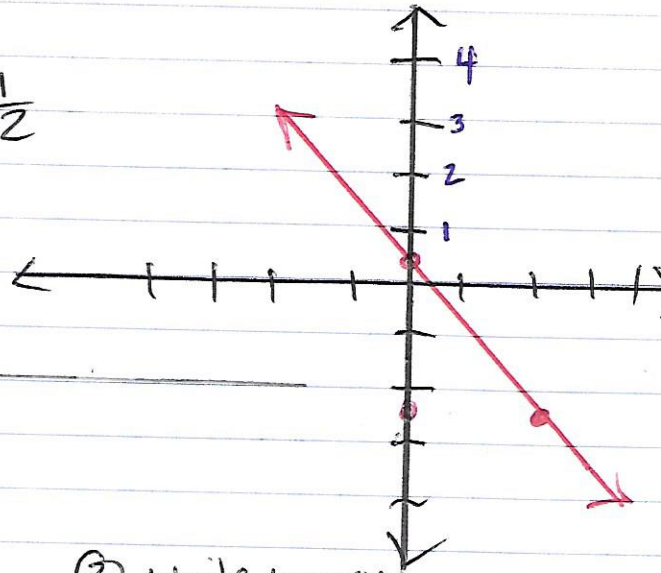


14.

$$y = -\frac{3}{2}x + \frac{1}{2}$$

$$m = -\frac{3}{2}$$

$$b = \frac{1}{2}$$



15. Write in standard form

$$Ax + By = C$$

$m = -4; (2, 2)$

① find "b"

$$y = m \cdot x + b$$

$$2 = -4(2) + b$$

$$2 = -8 + b$$

$$\begin{array}{r} +8 \quad +8 \\ \hline 10 = b \end{array}$$

② write  $y = mx + b$   
 $y = -4x + 10$

so,

③ Change to standard form

$$\begin{array}{r} y = -4x + 10 \\ +4x \quad +4x \\ \hline 4x + y = 10 \end{array}$$

A, B, & C can't be fractions  $4x + y = 10$

16.  
 $m = \frac{2}{5}; (-1, 3)$

$$y - y_1 = m(x - x_1)$$

$$y - 3 = \frac{2}{5}(x + 1)$$

$$y - 3 = \frac{2}{5}x + \frac{2}{5}$$

$$\begin{array}{r} -\frac{2}{5}x \quad +3 \quad -\frac{2}{5}x \quad +3 \\ \hline \end{array}$$

$$-5 \left( -\frac{2}{5}x + y \right) = \left( \frac{17}{5} \right) (-5)$$

$$2x - 5y = -17$$

$$2x - 5y = -17$$



17.  
 $m=0; (3, -4)$

$$y - y_1 = m(x - x_1)$$

$$y + 4 = 0(x - 3)$$

$$y + 4 = 0$$

$$y = -4$$

$$y = -4$$

18. Find  
 slope & int.  
 $3x - 4y = 12$

$$3x - 4y = 12$$

$$\frac{3x - 4y}{-3x} = \frac{12}{-3x}$$

$$-4y = \frac{-3x + 12}{-4}$$

$$y = \frac{3}{4}x - 3$$

① Solve for y to find m

$$m = \frac{3}{4}$$

$$y\text{-int}$$

$$(0, -3)$$

intercepts.  $y\text{-int (b)}$

To find  $x\text{-int}$ :  
 substitute  $y$  for 0

$$3x - 4y = 12$$

$$3x - 4(0) = 12$$

$$\frac{3x}{3} = \frac{12}{3}$$

$$x = 4$$

$$x\text{-int}$$

$$(4, 0)$$

19.

$$y = -2$$

$y = -2$   $m = 0$   
 horizontal line  
 No  $x\text{-int}$   
 $y\text{-int (0, -2)}$

$$m = 0$$

$$\text{No } x\text{-int}$$

$$y\text{-int}$$

$$(0, -2)$$

20.  
 $f(x) = \frac{4}{5}x + 7$

$$m = \frac{4}{5} \quad y\text{-int} = (0, 7)$$

$$x\text{-int} \quad f(x) = \frac{4}{5}x + 7$$

$$0 = \frac{4}{5}x + 7$$

$$-7 = \frac{4}{5}x$$

$$\left(\frac{5}{4}\right) \cdot (-7) = \frac{4}{5}x \left(\frac{5}{4}\right) \quad x = -\frac{35}{4}$$

$$m = \frac{4}{5}$$

$$y\text{-int (0, 7)}$$

$$x\text{-int} \left(-\frac{35}{4}, 0\right)$$

21.  
 $x = 5$

Vertical line  $m = \text{und}$   
 $y\text{-int} \Rightarrow \text{None}$   
 $x\text{-int} \quad (5, 0)$

$m = \text{und}$   
 $y\text{-int} \Rightarrow \text{None}$   
 $x\text{-int} (5, 0)$

22. Write  
equ. & graph

$(-1, 3) \parallel$   
 $y = 2x + 1$

$y = 2x - 1 \quad m_1 = 2$   
 Since lines are  $\parallel$ , then  $m_2 = 2$

$$\begin{array}{r} y - y_1 = m(x - x_1) \\ y - 3 = 2(x + 1) \\ y - 3 = 2x + 2 \\ \hline y + 3 = 2x + 2 + 3 \\ \hline y = 2x + 5 \end{array}$$

$y = 2x + 5$

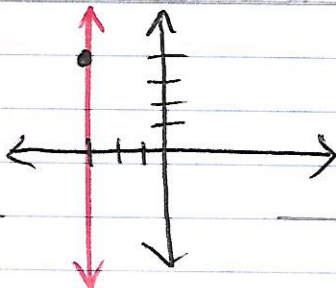
23.  $(2, 2)$   
 $\perp y = -\frac{3}{5}x + 2$

$m_1 = -\frac{3}{5} \quad m_2 = \frac{5}{3}$   
 $y - 2 = \frac{5}{3}(x - 2)$   
 $y - 2 = \frac{5}{3}x - \frac{10}{3}$   
 $\hline y = \frac{5}{3}x - \frac{4}{3}$

$y = \frac{5}{3}x - \frac{4}{3}$

24.  $(3, 4)$   
 & vertical

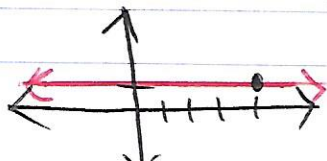
$x = -3$



$x = -3$

25.  $(4, 1)$   
 & horizontal

$y = 1$



$y = 1$